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# **Autoconstructive Evolution: Push, PushGP, and Pushpop**

Lee Spector  
Cognitive Science  
Hampshire College  
Amherst, MA 01002

lspector@hampshire.edu  
<http://hampshire.edu/lspector>

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# Overview

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**Autoconstructive Evolution**,  
self-construction of the evolutionary  
process

The **Push** programming language for  
evolutionary computation

**PushGP**, a genetic programming system  
that evolves Push programs

**Pushpop**, an autoconstructive  
evolution system that evolves Push  
programs

	Results	Potential (?)
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Push	*	*
PushGP	*	*
Pushpop	*	*

# **Autoconstructive Evolution**

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Individuals make their own children.

The machinery of reproduction and diversification (and thereby the machinery of evolution) evolves.

Radical self-adaptation.

# Making a living, Making babies

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Individuals, like natural organisms,  
must **both** make a living in the world  
and produce offspring.

.....

Making a living = performing well on a  
environment/problem-specific fitness  
test.

Producing offspring = generating code.

# Children

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Produced as output from parents' code.

Problem-solving and child-producing  
code may be integrated and  
interdependent.

May use arbitrary computational  
processes built in an expressive,  
Turing-complete programming language.

# Hypotheses

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Autoconstructive evolution systems can be valuable sources of data on the nature of life and evolution.

Autoconstructive evolution systems can out-perform traditional evolutionary computation systems by adapting their reproductive mechanisms to their representations and problem environments.

# Advance praise for the Push programming language

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*Multiple data types with **no** constraints on code generation or manipulation!* (Compare to Strongly Typed Genetic Programming [Montana].)

*Arbitrary modularity with **no** constraints on code generation or manipulation!* (Compare to Automatically Defined Functions [Koza] or Automatically Defined Macros [Spector].)



*You'll **never** need to pre-specify the module architecture! **No** extra machinery required for architecture evolution!* (Compare to Architecture-Altering Operations [Koza].)

*Explicit and arbitrary recursion? **No problem!*** (in principle) (Compare to the work of Yu and others)

*Ontogenetic development, evolved adaptivity, and diversifying self-replication? **Push makes it easy!*** (in principle) (Compare to Ontogenetic Programming [Spector], TIERRA [Ray], Avida [Adami].)

# The Push programming language for evolutionary computation

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Goals:

- multiple data types
- modularity
- Turing completeness
- recursion
- code manipulation
- **uniform syntax**

# Push

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Stack-based, like Forth or Postscript

Multiple stacks, one for each type

Types are hierarchical

**Type** constants on a **type** stack/bottom

Missing argument? NOOP

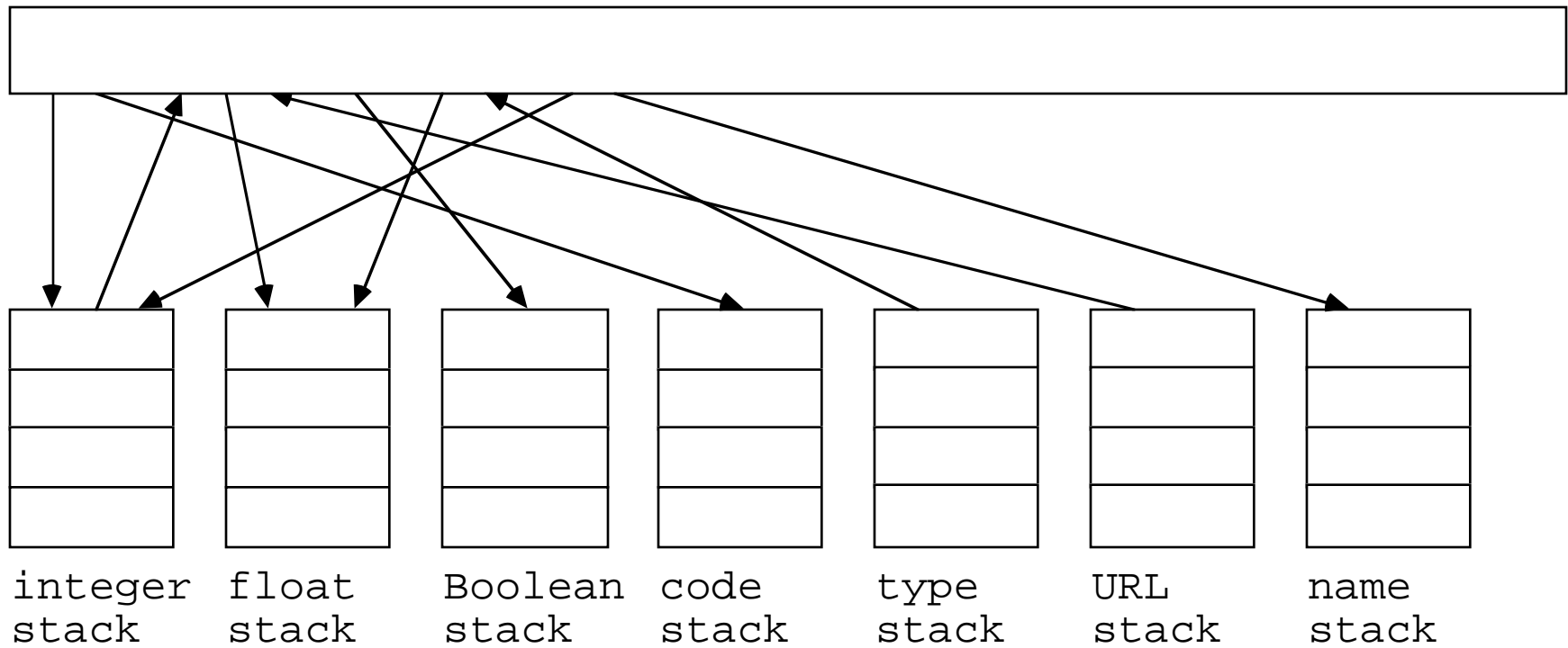
**Code** type/stack -> advanced features

Runtime resource limits

# Push architecture

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possibly nested program of stack-manipulating instructions



more stacks as needed

# Push examples

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```
(integer 2 3 +)
```

```
(integer 2 3 + float 2.72 3.14 +)
```

```
(2 3 2.72 3.14 integer + float +)
```

```
(2.72 integer 2 3.14 3 + float +)
```

```
((integer) (2 (3)) +)
```

```
(code quote (integer 2 3 +) do)
```

# Factorial in Push

.....

```
(quote (pop 1)
  quote (code dup
    integer dup
    1 - do *)
integer dup 2 < if)
```

# Factorial with Names

.....

```
(code
  quote (quote (pop 1)
    quote (integer dup 1 -
      code factorial get do
        *)
    integer dup 2 < if)
  factorial set
  factorial get do)
```

# The Push type hierarchy

- .....
- push-base-type: dup, pop, swap, rep, =[boolean],  
                  set[name], get[name], convert[type],  
                  pull[integer], noop
  - number: +, -, \*, /, >[boolean], <[boolean]
    - integer: rand, pull, /
    - float: rand
  - boolean: not, and, or, nand, nor, rand
  - expression: quote, car, cdr, cons, list, append, subst,  
              container, length[integer], size[integer],  
              atom[boolean], null[boolean], nth[integer],  
              nthcdr[integer], member[boolean],  
              position[integer], contains[boolean],  
              insert[integer], extract[integer],  
              instructions[type], perturb[integer],  
              other[integer], other-tag[float],  
              elder[integer], neighbor[integer],  
              rand[integer]
    - code: do, do\*, if[boolean], map
    - child:
  - type: rand
  - name: rand

Inheritance, multi-stack access, subsets



# **PushGP: GP for Push programs**

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≈ Standard Koza-style GP but evolves  
Push programs

Uniform code generation

Crossover: expression swapping or  
uniform crossover on terminals

Mutation: replacement, perturbation

Tournament selection.

Networked on a 16-node cluster.

# PushGP: symbolic regression

[Robinson, 2001]

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Cases	50 from $x^6 - 2x^4 + x^2$
Popsiz	4000
Max Gens	51
Max Length	50 points
Instr Set	+ - * / dup ERC
Operators	90% xover, 10% duplication
Input	x value on integer stack
Fitness	Sum of error for all cases
Termination	error for each case < 0.01

One result:

(dup (dup dup \* (\*) - /) dup \*)

# PushGP: multiple data types and the ODD problem

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The ODD problem: Is a given integer  
odd? (integer->Boolean)

An odd solution:

```
((nth) atom (insert) pull)
```

Uses its own code as an auxiliary data  
structure.

Multiple data types can sometimes be  
used to synergistic advantage.

# **PushGP: PARITY and modularity**

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The EVEN PARITY problem: Is the number of "on" bits in the input even?  
(Boolean->Boolean)

EVEN PARITY can be decomposed into smaller parity problems; ADFs provide advantages [Koza].

# PushGP: solution (simplified) to EVEN 4-PARITY

.....  
(quote  
 (x x (x ((x) x)))  
 (list  
 (x)  
 ((x) (x quote (dup nand) if) nil)  
 (x x)  
 ((quote) ((x) x x) x (map nor))))

## Modular?

Recursive (via map)

Heavy code re-use (but not  
"human-style" !)

# PushGP results, continued

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Initial data on PushGP and larger parity problems: scaling of difficulty compares favorably with ADFs.

EVEN N-PARITY for bounded (but not yet unbounded)  $N$ .

Data/variants/comparisons to literature: Alan Robinson's thesis [Robinson, 2001]; also [Spector and Robinson, in preparation].

Real interest lies in application to new kinds of problems.

# **PushGP: current work**

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Unbounded recursion (e.g. factorial)

Seek human-competitive results in:

quantum computation

integer sequence induction

agents in virtual worlds

# **Pushpop: autoconstructive evolution of Push programs**

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Children: at the end of each program execution the top of the "child" stack is a potential child.

Selection: The children of the better parents are more likely to survive.

Sex: Access to code of other programs, for execution and/or reproduction. Access based on geography, fitness, and/or genetics. Any number of "genders" is possible.



# Pushpop: Diversity management

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Extreme measures are required.

Syntactic diversity: no clones

Semantic diversity:

Limit number of children from  
identically-performing parents

Vary fitness components  
geographically

Reproductive competence

## Pushpop: Results

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Reproductive competence is easily  
achieved.

Fitnesses generally improve.

Simple problems can be solved.

Evolutionary mechanisms evolve.

Some emergent features resemble those  
of natural and/or engineered self-  
adaptive systems, for example in the  
dynamics of reproductive strategies

Fitness-improvement often stagnates.

# What is necessary for the emergence of robust, fitness-progressive evolution?

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Hypotheses under exploration:

Spatial irregularity (neighbors,  
local climate, local problems)

Environmental dynamism (comets,  
seasons, climate change, cooling  
of the universe)

Thermodynamic constraints  
(information budgets)

# **Relations to TIERRA/Avida**

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Problem-solving orientation

Higher-level language

Fully endogenous diversification

# Summary/Conclusions

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Push supports novel evolutionary computation paradigms.

PushGP evolves Push programs to solve many types of problems. Modularity and other advanced programming features arise naturally.

Pushpop is an autoconstructive evolution system in which Push programs solve problems while constructing their own children and thereby their own evolutionary mechanisms.

# Cliffhangers

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Can Pushpop fulfill the hypothesized promise of autoconstructive evolution systems to out-perform traditional evolutionary computation systems by adapting their reproductive mechanisms to their representations and problem environments?

Can Pushpop fulfill the hypothesized promise of autoconstructive evolution systems to provide useful data on the nature of life and evolution?

***Come to GECCO-2002 (New York) to find out!*** (or maybe GECCO-2003 or 4 or...)